

# Studying the hybrid pulsator 12 Lacertae: mode identification and complex seismic modelling

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**Abstract** We present identification of the mode degree,  $\ell$ , for all observed frequencies of 12 Lac and results of seismic modelling which consists in fitting simultaneously the centroid mode frequencies and the corresponding values of the complex nonadiabatic  $f$ -parameter. Effects of chemical composition, opacities, core overshooting and non-LTE atmospheres were taken into account.

## 1 Mode identification

12 Lac is the early B-type pulsator in which at least ten frequencies of the  $\beta$  Cep type and one of the SPB type are excited. To determine the pulsation mode degree,  $\ell$ , we made use of the amplitudes and phases in the Strömgren  $uv$  photometric passbands [5] as well as the radial velocity data [4]. Two approaches were used: the first one with the theoretical  $f$ -parameter [2] and the second one with the empirical values of  $f$  [3]. The LTE [6] and non-LTE [7] stellar atmosphere models were included. We were able to find identification for five strongest modes and limitation on  $\ell$  for the others. The dominant mode  $\nu_1$  as well as  $\nu_2$  are certainly the dipole modes. Identification of  $\nu_3$  and  $\nu_5$  is also unique, they are quadruple modes, and  $\nu_4$  is a radial mode. The high-order g-mode is the dipole.

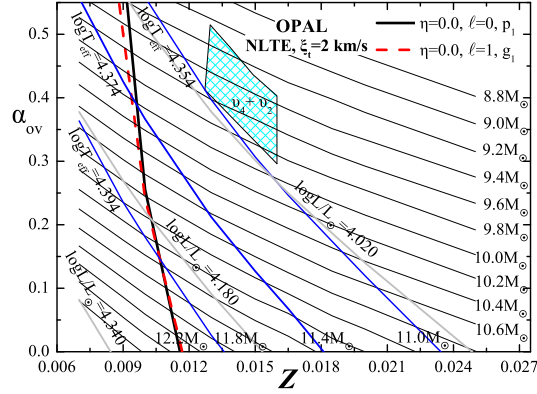
## 2 Seismic models of 12 Lac

We managed to construct models fitting simultaneously the two frequencies,  $\nu_4$  (the radial  $p_1$  mode) and  $\nu_2$  (the dipole  $g_1$  mode), and the corresponding values of the

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**Fig. 1** The OPAL seismic models of 12 Lac fitting  $v_2$  and  $v_4$  on the  $Z - \alpha_{ov}$  plane. The hatched area indicates models fitting the empirical  $f$ -parameter, simultaneously for  $v_4$  and  $v_2$ . The empirical values of  $f$  were calculated with the NLTE atmospheres.



$f$ -parameters. This approach is called complex asteroseismology and yields more information on model and theory. Calculations were performed in a wide range of metallicity, overshooting parameter from the convective core as well as for different stellar atmosphere models: LTE with the microturbulent velocity of 2 and 8 km/s, and NLTE with 2 km/s. We used the OPAL and OP opacity data, and the AGSS09 chemical mixture [1]. All effects of rotation were ignored. In Fig. 1, we give an example of seismic models obtained with the OPAL data on the  $Z - \alpha_{ov}$  plane.

### 3 Conclusions

Mode identification with the LTE and non-LTE atmospheres provided similar results. Comparison of the empirical and theoretical values of the nonadiabatic  $f$ -parameter allowed us to determine the radial order of the radial mode  $v_4$ . Clearly,  $v_4$  is the fundamental mode. With both opacity data we were able to construct seismic models fitting the  $v_4$  and  $v_2$  frequencies and the corresponding  $f$ -parameters. Moreover, models fitting the high-order g-mode frequency and reproducing its value of  $f$  were found. No preferences for any opacity tables were obtained.

### References

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